Beauty and the Beast
Toward a Measurement Framework for Example Program Quality

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UMINF-07.23
ISSN-0348-0542

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ABSTRACT
Examples are important tools for programming education. In this paper, we investi-
gate desirable properties of programming examples from a cognitive and a measure-
ment point of view. We argue that some cognitive aspects of example programs are
“caught” by common software measures, but they are not sufficient to capture all im-
portant aspects of understandability. We propose a framework for measuring the un-
derstandability of example programs that also considers factors related to the usage
context of examples.

Categories and Subject Descriptors
K.3 [Computers & Education]: Computer & Information Science Education - Computer Science Education.

General Terms
Design, Measurement.

Keywords
CS1, Programming Examples, Measurement, Understandability.
1. INTRODUCTION

Example isn’t another way to teach. It is the only way to teach. [A. Einstein]

Examples are important teaching tools. Research in cognitive science confirms that “examples appear to play a central role in the early phases of cognitive skill acquisition” [35]. More specifically, research in cognitive load theory has shown that alternation of worked examples and problems increase the learning outcome compared to just solving more problems [31, 32].

Students use examples as templates for their own work. Examples must therefore be easy to generalize. They must be consistent with the principles and rules of the topics we are teaching and free of any undesirable properties or behaviour. If not, students will have a difficult time recognizing patterns and telling an example’s superficial surface properties from those that are structurally important and of general importance.

Perpetually exposing students to “exemplary” examples, desirable properties are reinforced many times. Students will eventually recognize patterns of “good” design and gain experience in telling desirable from undesirable properties. Trafton and Reiser [32] note that in complex problem spaces, “[l]earners may learn more by solving problems with the guidance of some examples than solving more problems without the guidance of examples”.

With carefully developed examples, we can minimize the risk of misinterpretations and erroneous conclusions, which otherwise can lead to misconceptions. Once established, misconceptions can be difficult to resolve and hinder students in their further learning [8, 27].

But how can we tell “good” from “bad” examples? Can we measure the quality of an example?

2. PROPERTIES OF GOOD EXAMPLES

Any fool can write code that a computer can understand. Good programmers write code that humans can understand. [M. Fowler]

Programming is a human activity, often done in teams. About 40-70% of the total software lifecycle costs can be attributed to maintenance and the single most important cost factor of maintenance is program understanding [33]. That said, Fowler makes an important point in the quote above. In an educational context, this statement is even more important. In the beginning of their first programming course, students can’t even write a simple program that a computer can understand.

A good example must obviously be understandable by a computer. Otherwise it cannot be used on a computer and would therefore be no real programming example.

A good example must also be understandable by students. Otherwise they cannot construct an effective mental model of the program. Without “understanding”, knowledge retrieval works on an example’s surface properties only, instead of on its more general underlying structural properties [10, 32, 35].

A good example must also effectively communicate the concept(s) to be taught. There should be no doubt about what exactly is exemplified. To minimize cognitive load [25], an example should furthermore only exemplify one (or very few) new concept at a time.

The “goodness” of an example also depends on “external” factors, like the pedagogical approach taken. E.g., when our main learning goal is proficiency in object-oriented programming (in terms of concepts, not specific syntax), our examples should always be truthfully object-oriented and “exemplary”, i.e. they should adhere to accepted design principles and rules and not show any signs of “code smells” [12, 22, 28]. If examples are not consistently truthfully object-oriented, students will have difficulties picking up the underlying concepts, principles, and rules.

These three properties might seem obvious. However, the recurring discussions about the harmfulness or not of certain common examples show that there is quite some disagreement about the meaning of these properties [1, 38].

3. SOFTWARE MEASUREMENT

When you can measure what you are speaking about, and express it in numbers, you know something about it; but when you cannot measure it, when you cannot express it in numbers, your knowledge is of a meagre and unsatisfactory kind. [Lord Kelvin]

From our discussion in the previous sections, it would be desirable to find some way of determining the understandability of a programming example. A suitable measure could help us choose between existing examples and guide the development of new ones.

According to SEI’s quality measures taxonomy, understandability is composed of complexity, simplicity, structuredness, and readability [29]. Bansya and Davis [3] describe understandability as “[t]he properties of the design that enable it to be easily learned and comprehended. This directly relates to the complexity of the design structure”.

There are large bodies of literature on software measurement [4, 14, 26] and program comprehension [5, 6, 13, 21]. However, the work on software measurement focuses mainly on the structural complexity of software. There is only little work on measuring the cognitive aspects of complexity [7, 30]. The work on program comprehension focuses on the cognitive aspects, but is
mainly concerned with the comprehension process and not with software measurement.

4. ONE PROBLEM, TWO SOLUTIONS

Technical skill is mastery of complexity, while creativity is mastery of simplicity. 

[C. Zeeman]

Let us forget for a moment about actual software measures and look at two example programs for implementing a class Date, which could be part of some calendar application: the Beauty and the Beast.

Please note that we do not claim that these examples are either best or worse. They just exemplify a spectrum of design choices for object-oriented example programs targeted at novices, who are a few weeks into an introductory object-oriented programming course. Our examples could be easily criticized for exhibiting undesirable properties, like for example the possibility of creating invalid dates, insufficient commenting, or their lack of methods for doing this and that. Solving all these “shortcomings” might very well lead to better example programs, but definitely not to ones more easily understood by novices. Size actually matters. Adding more information and/or properties, even well-meant tips, will increase cognitive load, and will therefore very likely decrease understandability [35].

4.1 The Beauty

The Beauty (Figure 4-1) is developed according to sound principles of decomposition; we could call it extreme decomposition. The Beauty consists of four classes: Date, Month, and Year. A Date object knows its Day, Month, and Year. The three classes Day, Month, and Year are encapsulated as inner classes of the Date class, since they are not relevant to the surroundings. Their existence is a result of our choice of representation for class Date (see Figure 4-2).

The Beauty is beautiful for several reasons. First, there is an explicit representation of each of the key concepts in the problem domain. These can work as clues (so-called beacons) aiding in code comprehension [13]. Second, the interfaces and implementations of all classes are very simple and correspond closely to units in the problem domain. The solution therefore constitutes an easily recognizable distribution of responsibilities. Third, carefully chosen identifiers, matching problem domain concepts, enhance the readability of the code. Fourth, extreme decomposition reduces cognitive load by supporting independent and incremental comprehension, development, and test of each of the four component classes, as well as each of the methods in the classes.

```java
public class Date_Beauty {
    private Day day;
    private Month month;
    private Year year;

    public Date_Beauty(int y, int m, int d) {
        this.year = new Year(y);
        this.month = new Month(m);
        this.day = new Day(d);
    }

    public void setToNextDay() {
        day.next();
    }

    private class Day {
        private int d;   // 1 <= d <= month.days()
        public Day(int d) {
            this.d = d;
        }
        public void next() {
            d = d + 1;
            checkOverflow();
        }
        private void checkOverflow() {
            if ( d > month.days() ) {
                d = 1;
                month.next();
            }
        }
    } // Day

    private class Month {
        private int m;   // 1 <= m <= 12
        private final int[] daysInMonth=
            {0,31,28,31,30,31,30,31,31,30,31,30,31};
        /*  1  2   3  4  5  6  7  8  9 10 11 12 */
        public Month(int m) {
            this.m = m;
        }
        public int days() {
            int result= daysInMonth[m];
            if ( m == 2 && year.isLeapYear() ) {
                result = result + 1;
            }
            return result;
        }
        public void next() {
            m = m + 1;
            checkOverflow();
        }
        private void checkOverflow() {
            if ( m > 12 ) {
                m = 1;
                year.next();
            }
        }
    } // Month

    private class Year {
        private int y;
        public Year(int y) {
            this.y = y;
        }
        public void next() {
            y = y + 1;
        }
        public boolean isLeapYear() {
            return
                (isMultipleOf(4) && !isMultipleOf(100))
            || isMultipleOf(400);
        }
        private boolean isMultipleOf(int a) {
            return ( y % a ) == 0;
        }
    } // Year
    } // Date_Beauty
```

Figure 4-1: The Beauty
From the process point of view, The Beauty gives clues of how one could compose a complex program from simple units (methods and classes), focusing on one unit at a time.

A drawback of The Beauty is that one has to look into several classes to get the full picture of the solution. This problem can, however, be easily solved by providing a class diagram, like the one in Figure 4-2.

The Beast (Figure 4-3) is structured as one monolithic method. We could say it was developed according the principle of no decomposition.

class Date_Beast {  
    private int day; // 1 <= day <= days in month  
    private int month; // 1 <= month <= 12  
    private int year;  
    public Date_Beast(int y, int m, int d) {  
        day = d;  
        month = m;  
        year = y;  
    }  
    public void setToNextDay() {  
        int daysInMonth;  
        if ( month == 1 || month == 3 ||  
            month == 5 || month == 7 ||  
            month == 8 || month == 10 ||  
            month == 12 ) {  
            daysInMonth = 31;  
        } else {  
            if ( month == 4 || month == 6 ||  
                month == 9 || month == 11 ) {  
                daysInMonth = 30;  
            } else {  
                if ( year%4 == 0 && year%100 != 0  
                    || (year%400 == 0) ) {  
                    daysInMonth = 29;  
                } else {  
                    daysInMonth = 28;  
                }  
            }  
        }  
        day = day + 1;  
        if ( day > daysInMonth ) {  
            day = 1;  
            month = month + 1;  
            if ( month > 12 ) {  
                month = 1;  
                year = year + 1;  
            }  
        }  
        // setToNextDay()  
    }  
    // Date_Beast

The Beast has the advantage of collecting everything in one place. This leads to much less code in total. All necessary information is contained in a single statement sequence. The drawbacks are however numerous.

First, there is no explicit representation of the key concepts in the problem domain. Although this solution is much smaller than The Beauty, it is nevertheless difficult to get the full picture. It is not even possible to provide a high-level diagram to resolve that problem, since all processing is contained in a single method. Second, there is mainly one long statement sequence where everything is happening. Such an approach makes it impossible to introduce meaningful identifiers as clues (beacons) aiding in code comprehension. Third, the Beast shows no signs of “work units” or “chunks” of information. That makes it difficult to deconstruct the program and find appropriate starting points for a code comprehension effort. Fourth, The Beast is highly nested. Students have to keep track of many conditions at the same time, which increases cognitive load [25].

From the process point of view, The Beast does not lend itself as a pattern for incremental development and testing. Students might furthermore conclude that such a program is constructed as a large monolithic unit.

4.2 The Beast

4.3 Conclusion

Large, monolithic units of code are difficult to understand. To support code understanding a program should therefore be decomposed into suitable units\(^1\). Such decomposition will lead to a more complex design. One could say that in The Beauty the complexity (and thinking) went into the design. As a result, the units of code became simple. In The Beast the design is trivial, but the code is quite complex. In fact, there are very few simple units at all.

From an instructional design point of view, The Beauty has a big advantage over The Beast. In The Beauty, we are providing the difficult part (i.e. the design) and leave the simpler part to the students. In The Beast, on the other hand, the design is trivial, which leaves the more difficult part to the students. If we, as the educators, don’t consistently provide students with good role models for design, they will never be able to recognize patterns of “good” design. But with bad designs, they will always be left with unnecessarily difficult coding.

There is no doubt that solutions like the Beauty should be preferred. The Beauty is not only superior in structure, it is also superior from a learning theoretic point of view.

\(^1\) These units can be declarative, functional, or object-oriented. The Beast could for example be improved significantly without introducing further classes.
Small units reduce cognitive load [9, 25], structural similarities support the recognition of programming plans or patterns [6, 32, 35], and the frequent appearance of mnemonic names help to give meaning to program elements [10, 13].

The essence of developing programming examples is finding an appropriate structure that supports understanding, and hence learning. But when is one structure better than another? And how much better is it? Can we provide a yardstick for measuring the potential understandability of programs?

5. READABILITY AND UNDERSTANDABILITY

A basic prerequisite for understandability is readability. The basic syntactical elements must be easy to spot and easy to recognize. Only then, one can establish relationships between the elements. And only when meaningful relationships can be established, one can make sense of a program. Although readability is a component of understandability in SEI’s quality measures taxonomy [29] and there is a large body of literature on software measurement, we couldn’t find a single publication on measures for software readability.

5.1 The Flesch Reading Ease Score

The Flesch Reading Ease Score (FRES) is a measure of readability of ordinary text [11, 36]. Based on the average sentence length (words/sentences) and the average word length (syllables/words) a formula is constructed to indicate the grade level of a text. Lower values of the ratios indicate easy to read text and higher values indicate more difficult to read text. I.e. the shorter the sentences and words in a text, the easier it is to read.

Please note that FRES does not say anything about understandability. The FRES is just concerned with “parsing” a text. Its understanding depends on further factors, like for example familiarity of the actual words, sentence structure, or reader interest in the text’s subject.

Flesch’s work was quite influential and has been applied successfully to many kinds of texts. There are also measures for other languages than English.

5.2 A Reading Ease Score for Software

Following the idea of Flesch, we propose a Software Readability Ease Score (SRES) by interpreting the lexemes of a programming language as syllables, its statements as words, and its units of abstraction as sentences.

We could then argue that the smaller the average word length and the average sentence length, the easier it is to recognize relevant units of understanding (so-called “chunks” [9, 15, 24, 25]).

A chunk is a grouping or organization of information, a unit of understanding. Chunking is the process of reorganizing information from many low level “bits” of information into fewer chunks with many “bits” of information [24]. Chunking is an abstraction process that helps us to manage complexity. Since abstraction is a key computing/programming concept [2, 16, 19], proper chunking is highly relevant for the understanding of programming examples.

Clearly, there are other factors influencing program readability, like for example control flow, naming, and how much the students have learned already. We will come back to these factors in our discussion section. For a good overview over code readability issues, see [10].

5.3 Documentation

Documentation can be in the form of comments in the software itself and/or auxiliary information, like design descriptions. From a software engineering point of view, documentation is a key factor for software understandability. However, with respect to instructional design, we get a different picture. Research on worked examples and cognitive load suggests that programming examples need to be documented very carefully to avoid negative effects on learning [34]. For example, when integrating multiple sources of information cognitive load can usually be decreased, since the learners can more easily focus on the important part(s) of an example. However, when redundant information is integrated cognitive load can actually increase. For novices, it seems difficult to just ignore integrated redundant information [34].

6. MEASURING UNDERSTANDABILITY

As mentioned above, SRES only measures the readability of a program, i.e. how easy a program is parsed by a human. Readability is necessary but not sufficient for understanding a program. Other factors such as the structural and cognitive complexity also influence understanding. If we use cyclomatic complexity (CC) [23] as a measure of structural complexity and Halstead’s difficulty (D) [17] as a measure of cognitive complexity, and calculate these measures for the Beauty and the Beast, we get the figures as shown in the embedded table.

As indicated by the figures, the SRES measure is in favour of the Beauty. Even more so are the standard meas
ures of cyclomatic complexity and difficulty. This indicates that understandability indeed could be measured (if we accept that the Beast actually is more difficult to understand than the Beauty).

Of course, this is just an example; the programs we measure as well as the measures we apply are more or less randomly chosen among countless options (see for example [4, 14, 26]). To expand our investigation a bit, we have investigated a number of other standard measures, and we have extended the suite of program examples.

The measures we have investigated have been selected for their reported significance in the literature; the selected measures are presented in Table 1.

<table>
<thead>
<tr>
<th>Measure</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>LoC</td>
<td>Total lines of code.</td>
</tr>
<tr>
<td>SRES</td>
<td>Maximum cyclomatic complexity (CC) of methods (m); the number of (statically) distinct paths through a method; should be ≤10 [23].</td>
</tr>
<tr>
<td>CCmax(m)</td>
<td>Difficulty of a program, based on its number of operators and operands [17].</td>
</tr>
<tr>
<td>avgV(c), avgCC(c), avgLOC(c)</td>
<td>Factors of the Maintainability Index, a measure with high predictive value for software maintainability [37]. The measures report average values for Volume, V (size in terms of the numbers operators and operands [17]), CC, and LoC per class (c).</td>
</tr>
<tr>
<td>CC/LoC</td>
<td>Average CC per LoC, where CC is the sum of the cyclomatic complexities of all methods; should be ≤0.16 [20].</td>
</tr>
<tr>
<td>LoC/m</td>
<td>Average LoC per method, where m is the number of methods; should be ≤7 [20].</td>
</tr>
<tr>
<td>m/c</td>
<td>Average number of methods per class, where m and c are the number of methods and classes, respectively; should be ≤4 [20].</td>
</tr>
<tr>
<td>WMC</td>
<td>Weighted Method Count, the product of the three previous measures; should be ≤5 [20].</td>
</tr>
</tbody>
</table>

Table 1: Selected candidate measures for understandability.

The suite of program examples is extended from two to five representing a continuum of programs solving the Date problem: Beauty (E1), Good (E2), Bad (E3), Ugly (E4), Beast (E5). E2 is the same as E1 except that daysInMonth is handled by nested if’s. E3 is the same as E2 except that the classes are not nested. E4 is the same as E3 except that setToNextDay is decomposed into helper methods.

The result of our investigation is captured in Table 2. For all measures, lower values are considered better. Threshold values suggested in the literature are given in column T.

<table>
<thead>
<tr>
<th>Measure</th>
<th>T</th>
<th>E1</th>
<th>E2</th>
<th>E3</th>
<th>E4</th>
<th>E5</th>
</tr>
</thead>
<tbody>
<tr>
<td>LoC</td>
<td>50</td>
<td>59</td>
<td>57</td>
<td>31</td>
<td>32</td>
<td></td>
</tr>
<tr>
<td>SRES</td>
<td>±42</td>
<td>10.3</td>
<td>8.9</td>
<td>9.3</td>
<td>11.9</td>
<td>16.2</td>
</tr>
<tr>
<td>CCmax(m)</td>
<td>10</td>
<td>3</td>
<td>7</td>
<td>7</td>
<td>7</td>
<td>17</td>
</tr>
<tr>
<td>D</td>
<td>7.92</td>
<td>7.15</td>
<td>9.71</td>
<td>22.4</td>
<td>43.2</td>
<td></td>
</tr>
<tr>
<td>avgV(c)</td>
<td>387</td>
<td>412</td>
<td>363</td>
<td>752</td>
<td>798</td>
<td></td>
</tr>
<tr>
<td>avgCC(c)</td>
<td>10</td>
<td>4.8</td>
<td>6.25</td>
<td>5.25</td>
<td>14.0</td>
<td>18.0</td>
</tr>
<tr>
<td>avgLoC(c)</td>
<td>12.5</td>
<td>14.8</td>
<td>14.3</td>
<td>31.0</td>
<td>32.0</td>
<td></td>
</tr>
<tr>
<td>CC/LoC</td>
<td>0.16</td>
<td>0.4</td>
<td>0.42</td>
<td>0.37</td>
<td>0.45</td>
<td>0.56</td>
</tr>
<tr>
<td>LoC/m</td>
<td>7</td>
<td>2.9</td>
<td>3.27</td>
<td>4.09</td>
<td>6.75</td>
<td>14.0</td>
</tr>
<tr>
<td>m/c</td>
<td>4</td>
<td>3.3</td>
<td>3.75</td>
<td>2.75</td>
<td>4.0</td>
<td>2.0</td>
</tr>
<tr>
<td>WMC</td>
<td>5</td>
<td>3.6</td>
<td>5.2</td>
<td>4.1</td>
<td>12.2</td>
<td>15.8</td>
</tr>
</tbody>
</table>

Table 2: Values of selected measures for sample programs.

7. DISCUSSION

Although the measures focus on different aspects of a program, it can be noted that they “favour” programs with high degrees of decomposition (E1–E4). This is not surprising, since all research in software design and measurement proposes decomposition as a tool to manage complexity. In relation to education it is important to note that a high degree of decomposition also is an advantage from a cognitive point of view.

However, there are many important aspects of understandability not covered by any measure, like for example the choice of names, commenting rate, etc. Any example must furthermore take into account the educational context, i.e. what the students already (are supposed to) know.

8. A MEASUREMENT FRAMEWORK

From the literature and our discussion above, we conclude that understandability is a complex concept that cannot be captured by a single measure. It would therefore be useful to define simpler basic measures to capture as many aspects as possible of understandability.

Since our context here is teaching and learning, we also need to emphasize instructional design. We therefore also have to consider factors related to the context of example use.

Such a factorization would make it much easier to argue about the many facets of understandability. A perfectly structured program can very well be difficult to understand, when all identifiers are chosen badly. Furthermore, perfect values for all example factors are no guarantee for an understandable program, when students have not yet been introduced to the concepts used in the example.
Group 1 measures. These measures are all objective program measures independent of the educational context.

- **Readability**: Captures how easy a programming text is to read, based on SRES or similar measures (see section 5.2).
- **Structural complexity**: Captures the structural properties of an example program, based on measures for control flow complexity, coupling, cohesion, etc. (see for example [4, 14, 23, 26]).
- **Cognitive complexity**: Captures the effects of cognitive load caused by the amount of information contained in the “chunks” of an example program. Cognitive complexity is only partly covered by existing measures (see for example [7, 17, 18, 30]).
- **Commenting**: Captures how well an example program is commented.
- **Size**: Captures the size of an example program, based on a common size measure, like for example LoC or the number of executable statements.

Group 2 measures. These measures are still objective program measures, but they depend on the educational context. Guidelines and rules are for example not universally accepted. Measurement can therefore only be relative to guidelines and rules used/taught in a particular educational context.

- **Consistency**: Captures how well an example program follows accepted design principles and rules.
- **Presentation**: Captures the degree of conformance to a style guide or standard or the similarity of style with other examples.

Measures for consistency and presentation could for example be based on the number of “smells” with respect to violations of guidelines, rules or styles. To capture factors related to instructional design, one could define specific “educational smells” in accordance with Fowler’s “code smells” [12]. There is a range of tools that could be used to evaluate such violations, like for example PMD\(^2\) or Checkstyle\(^3\).

Group 3 measures. These measures depend on a program’s context. They take into account how an example is used.

- **Vocabulary**: Captures the familiarity of the names occurring in an example. Identifiers are important beacons during program comprehension [13]. Concepts should be named unambiguously to avoid confusion. It seems therefore advisable to “reuse” terms from the problem or example description in the code. Suitable measures could for example consider the size of the vocabulary and “reuse factor” of identifiers.
- **Progression**: Captures how well an example “fits” with what the students (are supposed to) know. This factor is most difficult to measure, because it depends on the short term learning goals for a particular example program. However, there are also general educational aspects, like the number of new concepts introduced, that could be considered.

For the group 3 measures, more research into the learning sciences is necessary to define suitable and more concrete actual measures.

9. CONCLUSION AND FUTURE WORK

In this paper, we have discussed understandability of example programs from a cognitive and a measurement point of view. We argue that common software measures are not sufficient to capture all relevant aspects of understandability of example programs. To be useful in an educational context such measures should emphasize factors like cognitive load and instructional design to a higher degree.

We also propose and discuss a new measure for software readability (SRES). We conclude that all these measure, although useful, lack in their disregard of factors related to the usage of examples. Based on our discussion, we propose a framework for measuring the understandability of programming examples that aims to take such factors into account.

In future research we aim at fine-tuning and empirically validating our measurement framework by studying a wide variety of example programs from introductory programming textbooks and course materials.

10. REFERENCES


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